

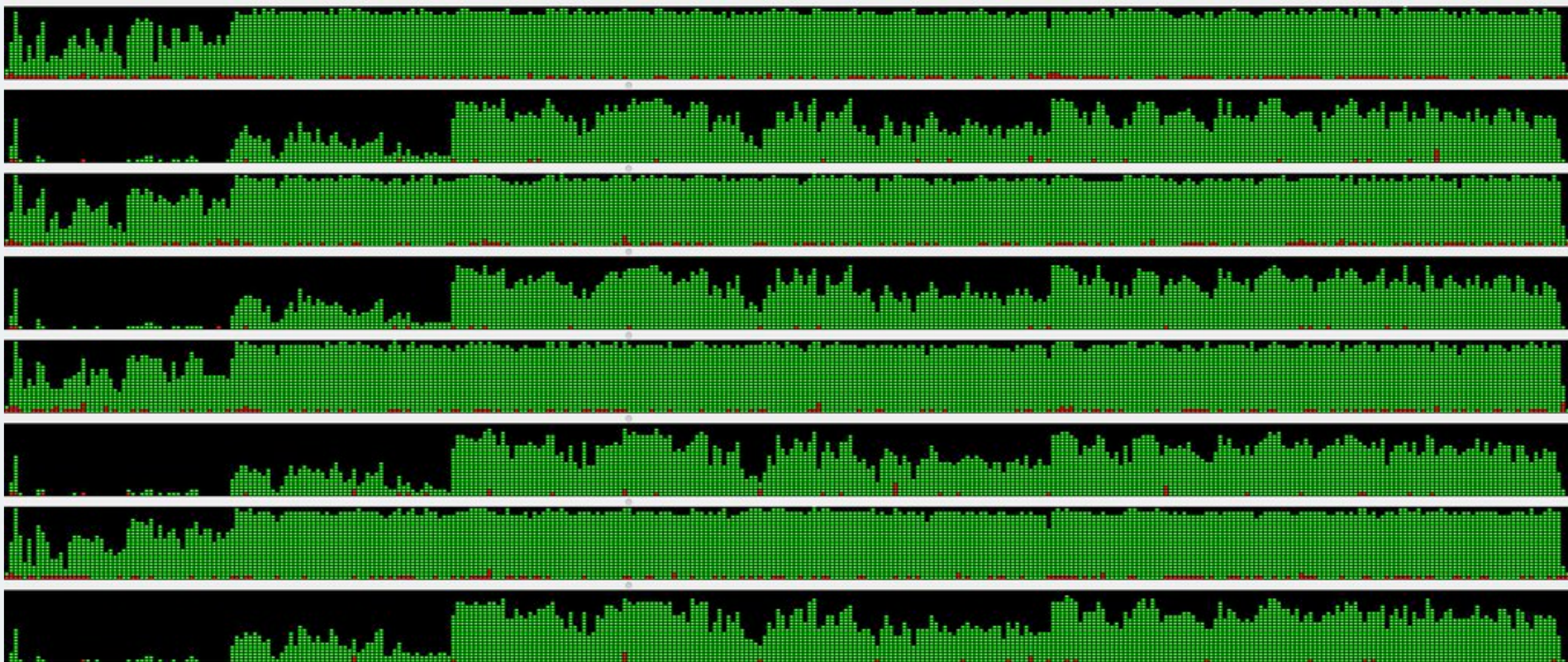
Turbo Charge CPU Utilization in Fork/Join Using the ManagedBlocker

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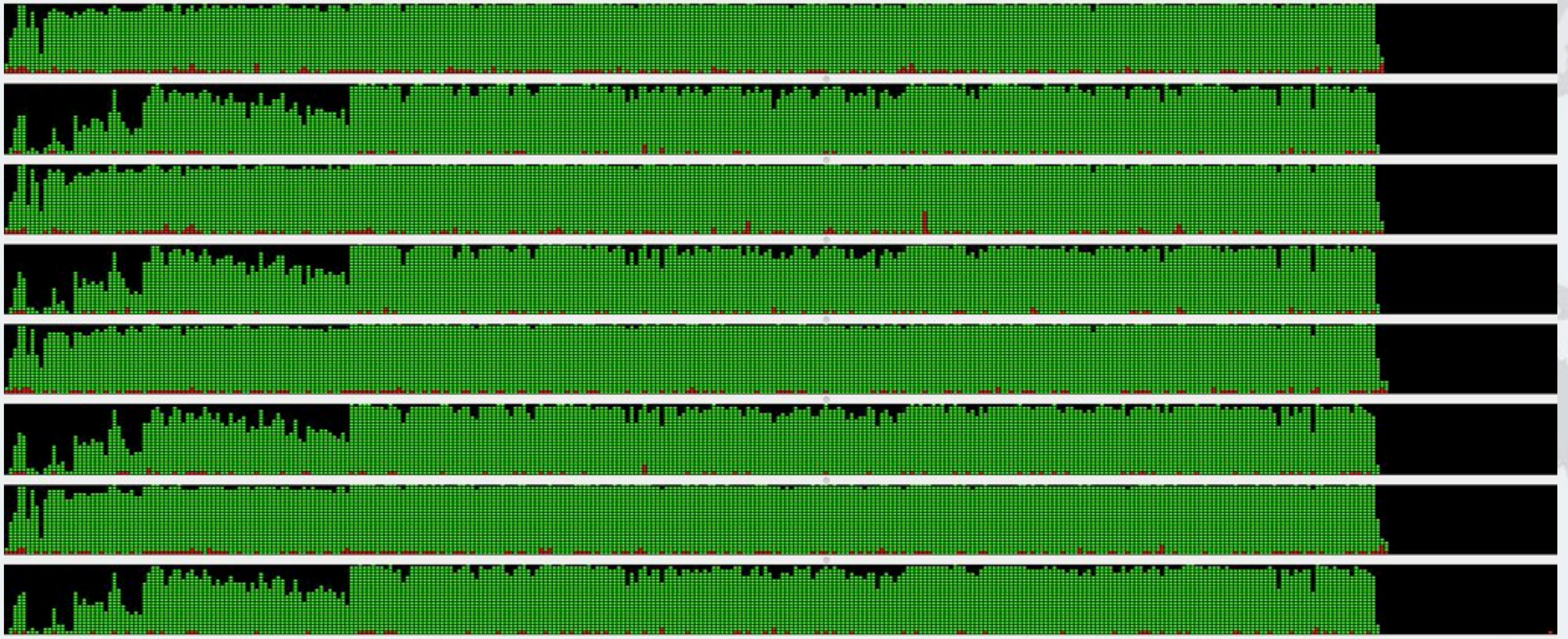
Last Updated 2017-01-24



Regular



ManagedBlocker



Speeding Up Fibonacci

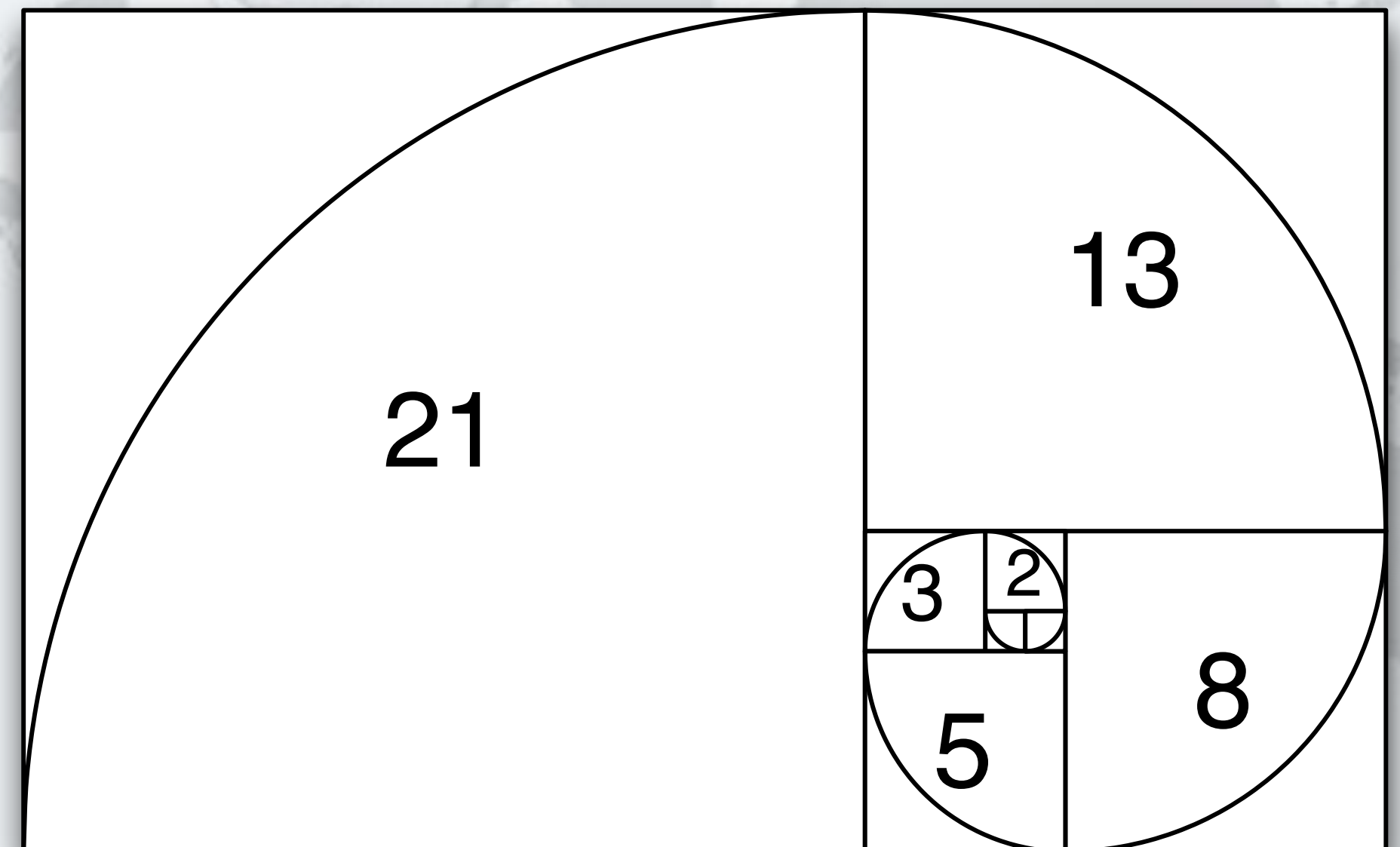
- **Number sequence named after Leonardo of Pisa**

- $F_0 = 0$
- $F_1 = 1$
- $F_n = F_{n-1} + F_{n-2}$

- **Thus the next number is equal to the sum of the two previous numbers**

- e.g. 0, 1, 1, 2, 3, 5, 8, 13, 21, ...

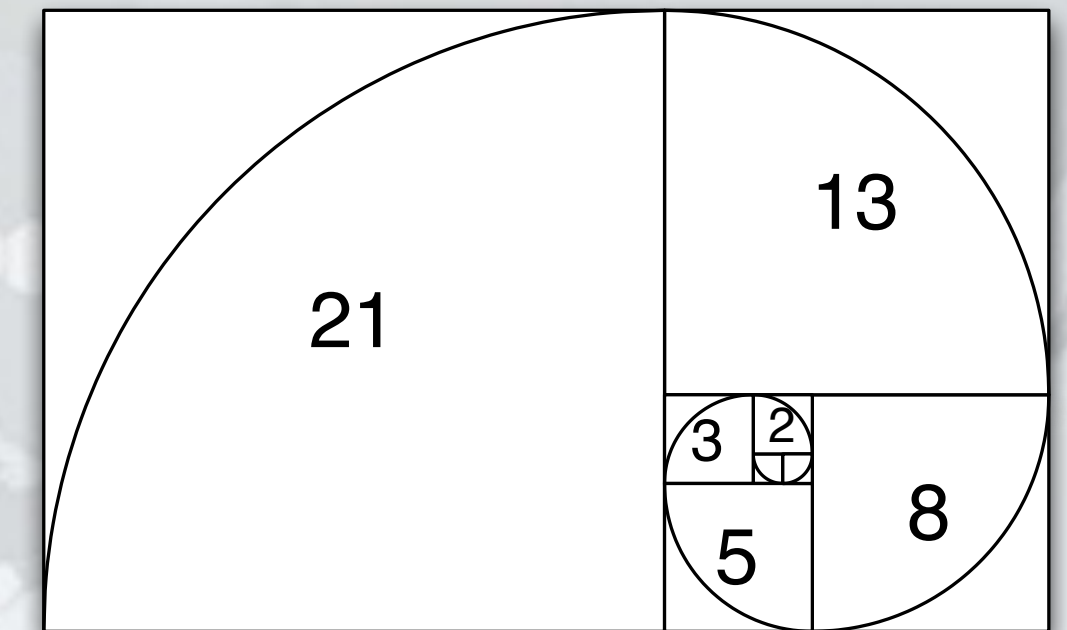
- **The numbers get large very quickly**



First attempt at writing a Fibonacci Method

- **Taking our recursive definition**

- $F_0 = 0, F_1 = 1$
- $F_n = F_{n-1} + F_{n-2}$



- **Our first attempt writes a basic recursive function**

```
public long f(int n) {  
    if (n <= 1) return n;  
    return f(n-1) + f(n-2);  
}
```

- **But this has exponential time complexity**

- $f(n+10)$ is 1000 slower than $f(n)$

2nd Attempt at Coding Fibonacci

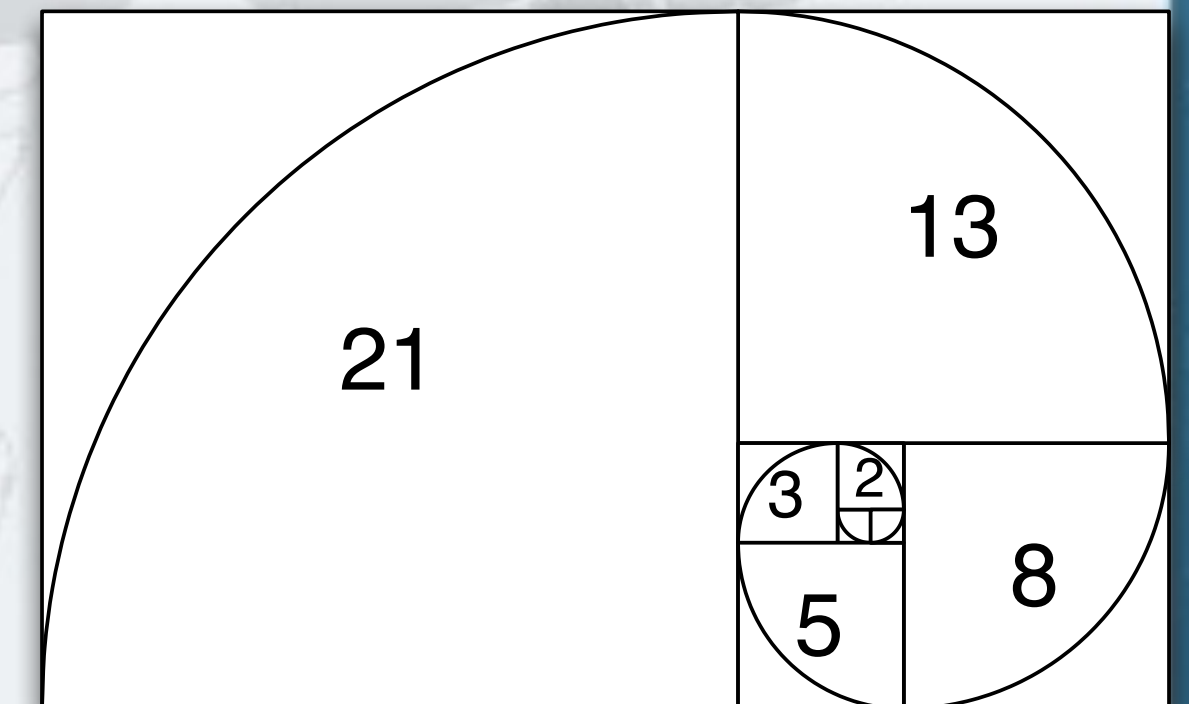
- **Instead of a recursive method, we use iteration:**

```
public static long f(int n) {  
    long n0 = 0, n1 = 1;  
    for (int i = 0; i < n; i++) {  
        long temp = n1;  
        n1 = n1 + n0;  
        n0 = temp;  
    }  
    return n0;  
}
```

- **This algorithm has linear time complexity**

- **Solved $f(1_000_000_000)$ in 1.7 seconds**

- **However, the numbers overflow so the result is incorrect**
- **We can use BigInteger, but its `add()` is also linear, so time is quadratic**
- **We need a better algorithm**

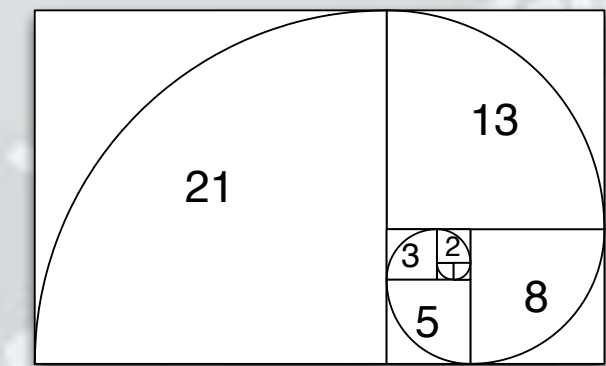


3rd Attempt Dijkstra's Sum of Squares

- **Dijkstra noted the following formula for Fibonacci**

- $F_{2n-1} = F_{n-1}^2 + F_n^2$

- $F_{2n} = (2 \times F_{n-1} + F_n) \times F_n$



- **Logarithmic time complexity and can be parallelized**

- Java 8 uses better BigInteger multiply() algorithms

- Karatsuba complexity is $O(n^{1.585})$

- 3-way Toom Cook complexity is $O(n^{1.465})$

- Previous versions of Java had complexity $O(n^2)$

- Unfortunately multiply() in BigInteger is only available single-threaded - we'll fix that later

Demo 1: Dijkstra's Sum of Squares

- **We implement this algorithm using BigInteger**
 - $F_{2n-1} = F_{n-1}^2 + F_n^2$
 - $F_{2n} = (2 \times F_{n-1} + F_n) \times F_n$

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Demo 2: Parallelize Our algorithm

- **We can parallelize by using common Fork/Join Pool**

```
private final class FibonacciTask extends RecursiveTask<BigInteger> {  
    private final int n;  
    private FibonacciTask(int n) {  
        this.n = n;  
    }  
    protected BigInteger compute() {  
        return f(n);  
    }  
}
```

- **Next we fork() the 1st task, do the 2nd and then join 1st**

```
FibonacciTask fn_1Task = new FibonacciTask(n - 1);  
fn_1Task.fork();  
BigInteger fn = f(n);  
BigInteger fn_1 = fn_1Task.join();
```

Demo 3: Parallelize BigInteger

- **Using principles from demo 2, we now parallelize methods in `eu.javaspecialists.performance.math.BigInteger`**
 - `multiplyKaratsuba()`
 - `multiplyToomCook3()`
 - `squareKaratsuba()`
 - `squareToomCook3()`

Demo 4: Cache Results

- **Dijkstra's Sum of Squares needs to work out some values several times. Cache results to avoid this.**



Demo 5: Reserved Caching Scheme

- **We make sure we implement a “reserved caching scheme” where if one thread says he wants to calculate some value, others would wait**
 - e.g. have a special BigInteger that signifies **RESERVED**
 - First thing a task would do is check if map contains that
 - If it doesn't, it puts it in and thus reserves it
 - If it does, it waits until the task is done and uses that value

Demo 6: ManagedBlocker

- **ForkJoinPool is configured with *desired parallelism***
 - Number of active threads
 - ForkJoinPool mostly used with CPU intensive tasks
- **If one of the FJ Threads has to block, a new thread can be started to take its place**
 - This is done with the ManagedBlocker
- **We use ManagedBlocker to keep parallelism high**

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